

## Kid-RSA

Kid-RSA is a public-key cipher system proposed by Neal Koblitz for pedagogic purposes. It is an asymmetric cryptosystem similar to RSA, but is simpler than RSA.

### 1. Setup

A person (Alice) chooses four numbers  $a$ ,  $b$ ,  $a_1$ ,  $b_1$ . Then Alice sets

- $M = a * b - 1$
- $e = a_1 * M + a$
- $d = b_1 * M + b$
- $n = (e * d) / M$

Now Alice Public key  $(n, e)$  and her private key is  $(n, d)$ .

To send Alice a plaintext  $P$ , one uses the function  $C = e * P \pmod{n}$ .

Then Alice can decipher the ciphertext by using the function  $P = C * d \pmod{n}$ .

Note: The plaintext has to be a number in the range of 0 to  $n-1$ . So for this system the plaintext or blocks of plaintext have to be converted into numbers in the range of 0 to  $n-1$ .

### Encryption and Decryption

To send Alice a plaintext  $P$ , one uses the function  $C = e * P \pmod{n}$ ;

Then Alice can decipher the ciphertext by using the function  $P = C * d \pmod{n}$ ;

Since Alice publishes  $e$  and  $n$ , any one who wants to send encrypted messages to Alice can do so, but these messages cannot be decrypted without the knowledge of  $d$ .  $d$  is kept as secret and only Alice knows it, so only she can decrypt messages.

### 2. Example

Let  $a = 9$ ,  $b = 11$ ,  $a_1 = 5$ ,  $b_1 = 8$

Therefore

$M$	$(a * b) - 1$	$(9 * 11) - 1$	98
$e$	$(a_1 * M) + a$	$(5 * 98) + 9$	499
$d$	$(b_1 * M) + b$	$(8 * 98) + 11$	795
$n$	$((e * d) - 1) / M$	$((499 * 795) - 1) / 98$	4048

Let the message be  $P = 538$ .

### Encryption

$$C = P * e \pmod{n} = 499 * 538 \pmod{4048} = 268462 \pmod{4048} = 1294$$

### Decryption

$$P = C * d \pmod{n}$$